363. Molecular Polarisability. The Molar Kerr Constants of Phenol and its p-Methyl, Chloro-, Bromo-, and Nitro-derivatives.

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The apparent dipole moments, molar Kerr constants, and certain other properties of the compounds mentioned in the title have been measured at 25° in carbon tetrachloride or benzene. Semi-axes of the corresponding polarisability ellipsoids are calculated, various bond data being used from previous work, and compared with results from experiment. Measurement and prediction are reconcilable if (a) in phenol and p-cresol the O-H link lies effectively slightly out of the plane of the Ar ring (either vibrating above or below this plane, or adopting fixed conformations, thus making the solutes mixtures of conformational isomers), and the resultant moments act at 60° or more to the C–O directions; and (b) in the other three compounds the molecules are effectively flat, and the resultant moments act at angles of ca. 45°, 37°, and 5° to the C-O direction.

As a result of recent work¹ on the n-alcohols it became of interest to enquire whether conclusions drawn therefrom regarding the polarisation and polarisability of the C-O-H unit could be applied satisfactorily to phenols. Accordingly, appropriate measurements were instituted on the five solutes named in Tables 1-3, and are here reported and discussed.

Experimental.—Materials and procedures. The solutes were redistilled or recrystallised immediately before use, steps being taken to keep them anhydrous. Benzene and carbon tetrachloride, as solvents, were also dry, being stored over sodium wire or calcium chloride respectively. Apparatus, procedures, methods of calculation, etc., were those standard among the Sydney group.^{2,3}

Results.—These are recorded under usual headings (see refs. 2—4 for definitions, explanations, etc.) in Tables 1-3.

TABLE 1. Kerr constants, refractivities, dielectric constants, and densities of mixtures containing weight fractions w₂ of solute at 25°.*

Phenol in carbon tetrachloride									
$10^5 w_2 \dots$	253	448	507		644	802	887	1118	
ε ²⁵	2.2398	$2 \cdot 2496$	2.252	4 2	2.2591	$2 \cdot 2665$	$2 \cdot 2710$	$2 \cdot 2814$	
d_{4}^{25}	1.58228	1.58107	1.580	45 1	$\cdot 57952$	1.57833	1.57780	1.57594	
$10^{4}\Delta n_{\rm D}$	4	6	6		7	10	13		
	1556	2470	286	3	2879	3715	5541		
ε ²⁵	$2 \cdot 3021$	$2 \cdot 3469$	2.367	8 2	2.3682	$2 \cdot 4124$	2.5164		
$d_{A^{25}}$	1.57289	1.56632	1.563	40 1	$\cdot 56222$	1.55718	1.54442		
$1\bar{0}^{4}\Delta n_{\mathbf{D}}$	22		41		42	53	76		
whence $\Delta \varepsilon = (5.15 \pm 0.02)w_2 + 24.3w_2^2$; $\Delta d = (-0.82 \pm 0.02)w_2 + 5.23w_2^2$; $\Sigma \Delta n / \Sigma w_2 = 0.1394$									
$10^5 w_2 \dots$	474	492	757	983	1076	1228	1525	1789	
$10^7 \Delta B$		0.012	0.027	0.036	0.040	0.051		0.068	
		whence $\sum (\Delta$	$B \cdot w_2) / \sum w_2$	$_{2}^{2} = 3.86$	$b_0; \Sigma \Delta B/2$	$\sum w_2 = 3.8$	08		
			p-Cresol in	ı carbon t	e trachl orid	le			
$10^5 w_2 \dots$	549	709	786		1075	1277	1286	1567	
ε ²⁵	2.2508	$2 \cdot 2577$	2.262	4 2	$2 \cdot 2745$	$2 \cdot 2829$	$2 \cdot 2830$	2.2964	
$d_{A^{25}}$	1.57981	1.57848	1.577	67]	1.57523	1.57364	1.57364	1.57107	
$1\bar{0}^4\Delta n_{\rm D}$	7	8				18	18		
$10^5 w_2 \dots$	1734	2133	2210)	2391	3022	3112	4041	
ε ²⁵	$2 \cdot 3040$	$2 \cdot 3209$	2.325	9 2	2.3323	$2 \cdot 3619$	$2 \cdot 3662$	2.4118	
d ₄ ²⁵	1.56992	1.56648	1.565	74]	1.56446	1.55927	1.55865	1.55109	
$10^4 \Delta n_{\mathbf{D}} \dots$	23	28			29	39	40	52	
whence $\Delta \varepsilon = (4.36 \pm 0.02)w_2 + 3.38w_2^2$; $\Delta d = (-0.872 \pm 0.003)w_2 + 1.24w_2^2$; $\Sigma \Delta n / \Sigma w_2 = 0.1294$									

¹ (a) Le Fèvre and Williams, *J.*, 1960, 108; (b) *ibid*, p. 115; (c) Le Fèvre and Rao, *J.*, 1960, 119; (d) Le Fèvre, Le Fèvre, Rao, and Williams, *J.*, 1960, 123; (e) Le Fèvre and Williams, *J.*, 1960, 128.

² Le Fèvre and Le Fèvre, J., 1953, 4041.
 ³ Le Fèvre and Le Fèvre, Rev. Pure Appl. Chem., 1955, 5, 261.
 ⁴ Le Fèvre, Le Fèvre, and Oh, Austral. J. Chem., 1957, 10, 218.

TABLE 1. (Continued.)									
$10^5 w_2 \dots$	923	963 1099		•			3086	3129 3	937 3939
$10^7 \Delta B$		0.025 0.028				0.054	0.075	0.076 0	·093 0·095
		whence $\sum (\Delta$	$(B \cdot w_2)/2$	$\sum w_2^2 = 2$	2·425; $\Sigma \Delta$	$\Delta B / \sum w_2 =$	2.444.		
p-Chlorophenol in carbon tetrachloride									
$10^5 w_2 \dots$	522	728		128	1142	115		1378	1427
ε^{25} d_{A}^{25}	$2 \cdot 2647 \\ 1 \cdot 58253$	$2 \cdot 2788$ $1 \cdot 58167$		6079 68039	$2 \cdot 3075 \\ 1 \cdot 58020$	2·308 1·580		2.3257 1.57930	$2 \cdot 3286 \\ 1 \cdot 57938$
$10^4 \Delta n_{\mathbf{D}} \dots$				15		1500			21
$10^5 w_2 \dots$	1629	1704		440	2727	275		3484	4333
ϵ^{25} d_{a}^{25}	$2.3414 \\ 1.57851$	$2.3472 \\ 1.57820$		1888 17535	$2 \cdot 4078 \\ 1 \cdot 57456$	2·408 1·574		$2.4508 \\ 1.57188$	$2 \cdot 4958 \\ 1 \cdot 56864$
$10^4 \Delta n_{\mathbf{D}} \dots$	22	23			39		-	50	
whence $\Delta \epsilon$	= $(7 \cdot 41 \pm$	$(0.03)w_2 - 28$	$2w_{2}^{2};$ [$\Delta d = (-$	0.376 ± 0.00	$(003)w_2 +$	$0.23w_{2}^{2}$; $\sum \Delta n / \sum$	$w_2 = 0.1408$
$10^5 w_2 \dots$	346	516 780	93						
$10^7 \Delta B$	0.057	0.071 0.094						81 0.27	8 0.305
		whence Σ ($\Delta B \cdot w_2)_{i}$	$\sum w_{2}^{2} =$	$12 \cdot 2_6; \Sigma^2$	$\Delta B / \sum w_2 =$	$= 12.5_2$		
			p-Ch	lorophend	ol in benzen	ie			
$10^5 w_2 \dots$	1637	2074		131	3863				
ε^{25} d_4^{25}	$2 \cdot 3466 \\ 0 \cdot 87839$	2·3681 0·87963		188 38267	$2 \cdot 4570 \\ 0 \cdot 88477$	•			
•		$= (4.37 \pm 0.000)$				2795 + 0.	004)w, ·	$+ 0.13w_{2}^{2}$	
							, 2		
$10^5 w_2 \dots$	468	р- 960	*	епоі іп с. 064	arbon tetra 1216	cnioriae 13]	6	1573	1972
ϵ^{25}	2.2516	$2 \cdot 2764$		2822	2.2906	2.294		2.3081	2.3289
d4 ²⁵	1.58485			58530	1.58541	1.58	552	1.58574	1.58600
$10^{4}\Delta n_{\rm D}$	$\frac{3}{2278}$	2311		13 635	$\begin{array}{c} 15\\ 3026 \end{array}$	403	-	5504	29
$10^5 w_2 \dots w_2 \dots w_2$	2278 2.3438	2311 2·3442		8580	2.3768	2.42		2.4869	
d_4^{25}	1.58638			58652	1.58683	1.58		1.58887	
$10^4 \Delta n_{\rm D} \ldots$	33						-		0.1000
whence $\Delta \epsilon$	= (5.31 -	$(0.02)w_2 - 1$	$0.79w_2^2;$	$\Delta d = (0$	0.071 ± 0.0	$(01)w_2 + 0$	$0.12_5w_2^2$; $\sum \Delta n / \sum$	$w_2 = 0.1330$
$10^5 w_2 \dots$	312	691	713	966			194	1274	1553
$10^7 \Delta B \dots$ $10^4 \Delta n_D \dots$	0.040	0.082	0·085 9	0·11 11	5 0·1 11		138 17	$\begin{array}{c} 0.155 \\ 18 \end{array}$	$\begin{array}{c} 0.193\\ 20 \end{array}$
		whence Σ ($\Delta B \cdot w_2$	$(\sum w_{2}^{2}) =$	$12.0_7; \Sigma_4$	$\Delta B / \sum w_w =$	$= 12.0_{5}$		
$10^5 w_2 \dots$	575	589		625	708	92		1108	1446
ε^{25}	2.2926	2.2922		2936	$2 \cdot 2970$	2.30		2.3099	2.3238
d_4^{25}	0.87624		0.8	87638	0.87649			0.87841	0.87982
$10^{4}\Delta n_{\rm D} \dots 10^{5} w_{2} \dots$	$\begin{array}{c} 4\\1504\end{array}$	$\begin{smallmatrix}&2\\1527\end{smallmatrix}$	1	4 .636	$5 \\ 2142$	$\frac{8}{254}$		$\frac{8}{2742}$	$9\\4420$
ϵ^{25}	2.3249	2.3254		3279	2.3491	2.36		2.3683	2.4272
d ₄ ²⁵	0.88012		0.8	38070	0.88241	0.88		0.88530	0.89269
$10^4 \Delta n_{\rm D} \dots$	7	9	01 9.	8	12			17	22
whence Δ	$\varepsilon = (3.50)$	$\pm 0.03 w_2 + c$	$0.01w_2^2;$	$\Delta a = (0$	1403 ± 0.0	$(04)w_2 + 0$	$0.53w_{2}^{2};$	$\sum \Delta n / \sum n$	$w_2 = 0.0574$
105			-	*	ol in benzen				
$10^5 w_2 \dots w_2 \dots w_2 \dots w_2^{25} \dots \dots \dots \dots$	347 2.3300		517 5716 2	532 2·3759	$\begin{array}{c} 643 \\ 2 \cdot 4000 \end{array}$	$701 \\ 2.4085$	$712 \\ 2 \cdot 4112$	$2 2 \cdot 422$	
	0.87496			0.87527	0.87599	0.87611	0.8761		
$10^4 \Delta n_{\rm D} \ldots$	4				6	7			
$10^5 w_2 \dots$	908		79 707 (1073	1077	1113	1118		
ε^{25} d_{a}^{25}	2.4537 0.87682			2·4877 D·87730	$2 \cdot 4883 \\ 0 \cdot 87728$	$2 \cdot 4984 \\ 0 \cdot 87745$	$2 \cdot 4964 \\ 0 \cdot 8773$		
$10^4 \Delta n_D \dots$	7		8	9	10	10			
whence Δ	$\varepsilon = (18 \cdot 6)$	$\pm 0.6)w_2 + 14$	$4.9w_{2}^{2};$	$\Delta d = (0$	$\cdot 305 \pm 0.0$	$(001)w_2 + 2$	$2.01w_{2}^{2};$	$\sum \Delta n / \sum n$	$w_2 = 0.0617$
$10^5 w_2 \dots$	58	106	125	136	213		36	348	373
$10^{7}\Delta B$	0.050	0.109	0.120	0.130	0.20	9 0.5	847	0.380	0.376
$10^4 \Delta n_{\rm D} \ldots$		whence ∇t		Σ 101 2	109.9 · 5/		 . 101.¤	3	
whence $\sum (\Delta B \cdot w_2) / \sum w_2^2 = 102.9$; $\sum \Delta B / \sum w_2 = 101.5$. * Values at 25° when $w = 0$ are (a) for carbon tetrachloride $c = 2.9270$ $d = 1.58454$ $w_2 = -2.58454$									

* Values at 25° when $w_2 = 0$ are (a) for carbon tetrachloride, $\varepsilon = 2.2270$, d = 1.58454, $n_D = 1.4575$, $B = 0.070 \times 10^{-7}$; (b) for benzene, $\varepsilon = 2.2725$, d = 0.87378, $n_D = 1.4973$, $B = 0.410 \times 10^{-7}$.

TABLE 2.	Total j	polaris	ations at	infinite	dilution	, molecular
refraction	is, and	dipole	moments	calculat	ed from	Table 1.

Solute	Solvent	$(\alpha \varepsilon_1)_{w_2=0}$	$(\beta)_{w_2=0}$	$_{\infty}P_2$ (c.c.)	$R_{\mathbf{D}}$ (c.c.)	μ(d) *	μ (d) \dagger
C ₆ H₅·OH	CCl4	5.15	-0.517	77.5	28.0	1.56	1.53
Me∙C ₆ H₄•OH	CCl	4.36	-0.550	80·6 ₅	33.4	$1 \cdot 5_2$	1.49
Cl∙C ₆ H₄ OH	CCl_4	7.41	-0.237	130.1^{-1}	33.3	$2 \cdot 1_7^{-1}$	$2 \cdot 1_{6}$
,,	C ₆ H ₆	4.37	0.320	135.5	32.7	$2 \cdot 2_4$	$2 \cdot 2_{2}$
Br∙C ₆ H₄•OH	CCl ₄	5.31	0.045	127.6	36 ·0	$2 \cdot 1_2$	$2 \cdot 0_{95}$
,,	$C_{6}H_{6}$	3.50	0.461	145.7	37.5	$2 \cdot 3_0$	$2 \cdot 2_{8}$
NO₂•C ₆ H₄∙OH	C_6H_6	18.6	0.349	517.5	37.7_{5}	$4 \cdot 8_{4}$	$4 \cdot 8_{3}$

* The distortion polarisation being taken as $R_{\rm D}$, or \dagger as $1.05R_{\rm D}$.

TABLE 3. Molar Kerr constants at infinite dilution calculated from Tables 1 and 2.

			•			
Solute	Solvent	γ	δ*	δ **	$_{\infty}(_{\rm m}K_2)$ * \times 10	12 $_{\infty}(_{\rm m}K_2)$ ** \times 10 ¹²
C ₆ H ₅ •OH	CCl4	0.095	55.14	$54 \cdot 4_1$	$38 \cdot 1$	37.6
Me∙Č ₆ H₄∙OH	,,	0.088	34 ·6₄	34.9^{-}_{1}	27.6	27.7
Cl∙C₄H₄•OH	,,	0.096	$175 \cdot 2^{-1}$	178.9	166.4	170.0
Br•C ₆ H ₄ ·OH	,,	0.091	$172 \cdot 4$	$172 \cdot 2$	221.3	221.0
NO₂•Č₄Ĥ₄∙OH	C ₆ H ₆	0.062	250.9_{5}	247.7	2559	2524
* $(1/B_1) \sum (\Delta B$	$(w_2)/\sum w_2^2;$	** (1/B ₁)	$\sum \Delta B / \sum w_2;$	correspond	ing values of a	$_{\infty}(_{\rm m}K_2)$ are similarly
asterisked.						

DISCUSSION

Dipole Moments.—Earlier reported values for the present five solutes are not numerous and differ among themselves. They mostly refer to solutions in benzene, none to carbon tetrachloride as solvent. The M.I.T. Tables ⁵ list ranges as follows:

	μ (D)		μ (D)
Phenol	 1.41.7	p-Chlorophenol	$2 \cdot 1 - 2 \cdot 68$
p-Cresol	 1.57 - 1.64	<i>p</i> -Bromophenol	2.12_{5} - 2.86
		p-Nitrophenol	5.01 - 5.05

In particular, our results may be compared with those of Donle and Gehrekens⁶ who quote 1.57, 1.57, 2.22, 2.12₅, and 5.02 D, respectively, for the above molecules. Anzillotti and Curran⁷ give $\mu = 2.25$ D for p-bromophenol. Both Fogelberg and Williams⁸ and Donle and Gehrckens ⁶ record the moment of p-nitrophenol as slightly over 5 D.

Molar Kerr Constants.—An analysis of the observed values of ${}_{m}K$ is difficult because the conformation of the hydroxyl group and the direction of action of the molecular resultant moment (vis-à-vis the principal semi-axes of polarisability) are not known with certainty. The following approach to the problem leads to conclusions which roughly fit the data from experiment.

Le Fèvre and Rao⁹ listed semi-axes for benzene, toluene, chloro- and bromo-benzene, and nitrobenzene. Since $b_{\rm L}^{\rm C-H} = b_{\rm T}^{\rm C-H} = b_{\rm V}^{\rm C-H} = 0.064 \times 10^{-23}$ c.c., the corresponding semi-axes for "phenyl" or "p-X-phenyl" are known. Le Fèvre, Le Fèvre, Rao, and Williams determined the semi-axes of methanol $^{1(d)}$ as 0.315, 0.363, and 0.278 \times 10⁻²³; subtraction of $3b_i^{C-H}$ gives for the C-O-H fragment $b_1 = 0.123$, $b_2 = 0.171$, and $b_3 = 0.123$ 0.086×10^{-23} . If it is assumed that the respective semi-axes of the aryl group and the C-O-H unit are parallel, then estimates for the phenols emerge as in Table 4.

The totals, $\sum b_i$ (calc.) = $b_1 + b_2 + b_3$, computed on this basis, show satisfactory agreement in the first four cases with Σb_i (obs.) drawn from electronic polarisations taken as

⁵ Wesson, "Tables of Electric Dipole Moments," Technology Press, Massachusetts Inst. Technology, 1948.

⁶ Donle and Gehrckens, Z. phys. Chem., 1932, B, 18, 316.

 ⁷ Anzillotti and Curran, J. Amer. Chem. Soc., 1943, 65, 607.
 ⁸ Fogelberg and Williams, J. Amer. Chem. Soc., 1930, 52, 1356.

⁹ Le Fèvre and Rao, J., 1958, 1465.

TABLE 4. Predicted polarisability semi-axes.

	$10^{23}b_1$	$10^{23}b_2$	$10^{23}b_{3}$	$10^{23} \sum b_{i}$ (calc.)	$10^{23} \Sigma b_{ m i}$ (obs.)
H·C,H,OH	1.18	1.23	0.76	3.17	3.16
Me•Č _e H₄•OH	1.33	1.51	0.90	3.74	3.78
CŀC,H₄OH	1.54	1.36	0.84	3.74	3.76
Br•C ₆ H ₄ •OH	1.74	1.41	0.91	4.06	4.07
NO ₂ ·C ₆ H ₄ ·OH	1.68	1.31	0.88	3.87	4.26
$NO_2 \cdot C_6 H_4 \cdot OH$	(2.07)	1.31	0.88	4.26	4.26

 $0.95R_{\rm D}$, the values of $R_{\rm D}$ being those in Table 2. For p-nitrophenol $\sum b_i$ (obs.) $-\sum b_i$ (calc.) = 0.39×10^{-23} c.c. If, as previous work ⁹⁻¹¹ suggests, such exaltation of polarisability occurs predominantly along the 1,4 direction, then the semi-axes in the last line of Table 4 are probably more appropriate. The data of Table 4 correspond to values of $10^{35}\theta_1$ (the "anisotropy" term in the molar Kerr constant) as follow:

The problem now is the estimation of the θ_2 's (the "dipole" terms in the $_{m}K$'s). When the resultant moment μ_r acts in the plane containing b_1 and b_2 , and makes an angle α° with the b_1 direction, θ_2 is given by

$$\begin{aligned} \theta_2 &= (1/45 \mathbf{k}^2 T^2) [(b_1 - b_2)(\mu_r^2 \cos^2 \alpha - \mu_r^2 \sin^2 \alpha) + \\ & (b_2 - b_3)(\mu_r^2 \sin^2 \alpha) - (b_3 - b_1)(\mu_r^2 \cos^2 \alpha)] \end{aligned}$$

At the outset we thought α in phenol and p-cresol might be *ca*. 60° as in alcohols; ^{1(d)} however, this led to values of θ_2 which were too large (the *sums*, $\theta_1 + \theta_2$, from experiment being *ca*. 9 × 10⁻³⁵ for phenol and 7 × 10⁻³⁵ for *p*-cresol). Angles less than 60° diminished the disagreement:

The nearest approach to the observed values of θ_2 is given when $\alpha = 0^\circ$, but from the natures of the two molecules concerned this cannot be a correct result. With the more polar *para*-substituted derivatives the dependence of θ_2 on α is marked, θ_2 increasing as α is diminished. Values of α in harmony with our measurements are as follows:

That α might have such magnitudes in these three molecules seems credible; they are notably acidic, so that their X·C₆H₄·O portions are predisposed to become anions; two effects of this are predictable: the C-O-H angle may be increased (presumably in C-O-}H⁺ the three atoms are collinear) and resonance of the kind X·C₆H₄·O⁻ \longleftrightarrow X·C₆H₄=O will be favoured. Both effects will tend to move μ_{res} towards the 1,4 line; the presence in the 4-positions of groups having -M character will also assist the resonance mentioned.

With all five solutes we have initially assumed that contributions from forms such as ${}^{-}C_{6}H_{5} = \stackrel{+}{O}H$ cause the O-H bond to be coplanar with the Ar ring. Were this not so, however, for phenol and *p*-cresol an explanation of the foregoing unsuccessful calculations of θ_{2} for these substances would be forthcoming. As an illustration, suppose the C-O-H

¹¹ Ref. 3, p. 301.

¹⁰ Le Fèvre and Le Fèvre, J., 1954, 1577.

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unit to be in a plane normal to the Ar ring in phenol and p-cresol, then with μ_r at 60° to b_1 , $10^{35}\theta_2$ becomes -17.7 and -20.9 respectively; it is clear therefore that, as the O-H link is rotated about the C-O bond, out of the Ar plane, θ_2 will become less and less positive, and ultimately negative. There is of course no firm evidence that in these two molecules $\mu_{\rm res}$ is acting at 60° to b_1 . A simple vector calculation shows that the moment of phenol (1.53 D) needs to interact at 77° with the moment of toluene (0.34 D) to produce the resultant observed (1.49 D) for p-cresol. Use of 77° instead of 60° increases the negativities of the θ_2 's quoted. The observation of values of θ_2 lower than those calculated can thus be easily understood. Parallel considerations for the p-halogeno- and p-nitro-phenols are unnecessary because the quantities from experiment agree well enough with those from prediction and in no way suggest any need to reduce the latter.

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